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DEPARTMENT OF CIVIL ENGINEERING



PROJECT REPORT

ON

# **P-DELTA ANALYSIS OF BUILDING STRUCTURE**

In the partial fulfilment of requirements for the Bachelor's Degree in Civil Engineering. Subject Project-2 | Subject Code: CE(PROJ)882

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# SILIGURI ISTITUTE OF TECHNOLOGY

# **SILIGURI INSTITUTE OF TECHNOLOGY**

(A Degree Engineering Collage under TECHNO INDIA GROUP, Approved by AICTE and Affiliated to MAKAUT)

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## **CERTIFICATE**

This is to certify that the project report entitled "**P-Delta Analysis of Building structure**" submitted by "Sanjok Rai & Muskan Tamang" to the Siliguri Institute of Technology, Salbari, in partial fulfilment for the award of the degree of B. Tech in Civil Engineering is a bona fide record of project work carried out by them under my supervision. The contents of this report, in full or in parts, have not been submitted to any other institution or university for the award of any degree or diploma.

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## **ABSTRACT**

In structural engineering, the P-Delta effect refers to the abrupt changes in ground shear, overturning moment and the axial force distribution at the base of a sufficiently tall structure or structural component when it is subjected to a critical lateral displacement. The P-Delta effect is a second order effect, that is when a horizontal loading acts on a building causing it to deflect, the resulting eccentricity of the gravity loading from the inclined axes of the structure's vertical member causes the lateral displacements of the structure and the moments in the members to increase.

P-Delta analysis also known as second order analysis, It is a structural engineering analysis technique used to account for the effects of axial loads and deformations in building structures. It takes into consideration the geometric nonlinearity of a structure which becomes significant in tall or flexible structures. The name "P-Delta" comes from two main components:

- 1. "P" stands for axial loads (e.g., forces due to gravity, applied loads, or wind).
- 2. "Delta" represents the deformation or displacements caused by these loads.

In P-Delta analysis, the structural engineer considers how the deformations of a structure due to axial loads can in turn affect the distribution of forces and moments within the structure. This interaction between the applied loads and the resulting deformations is essential for accurately predicting the behavior and stability of tall buildings and other structures. Key factors for this analysis include building height, stiffness, and loading conditions. It is a critical part of the design of high rise buildings and other structures where second order effects are significant.

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## **INTRODUCTION**

## 1.1 General:

**P-Delta effect**, one type of geometric nonlinearity, involves the equilibrium compatibility relationships of a structural system loaded about its deflected configuration. Of particular concern is the application of gravity load on laterally displaced multi-story building structures.

P-Delta effect typically involves large external forces upon relatively small displacements. If deformations become sufficiently large as to break from linear compatibility relationships, then Large-Displacement and/or Large-Deformation analyses may become necessary. The two sources of P-Delta effect are illustrated in Figure 1, and described as follows:

- P-δ effect, or P-"small-delta", is associated with local deformation relative to the element chord between end nodes. Small P-delta effects can affect overall structural behaviour by slightly reducing the buckling load, and can change the moment within the member. Typically, P-δ only becomes significant at larger displacement values or in especially slender columns. Small P-delta effect is important for local buckling and for design algorithms that expect member buckling to be accounted for by analysis.
- P-Δ effect, or P-"big-delta", is associated with displacements of the member ends. Large P-delta effect is important for overall structure behaviour under significant axial load. As indicated intuitively by Figure 2, gravity loading will influence structural response under significant lateral displacement.



Fig 1.1.1: P-Delta about column



Fig 1.1.2: P-Delta about structure

# 1.2 Key Aspects of P-delta Analysis

**Nonlinear Geometry:** Considering the nonlinear relationship between displacements and forces, especially in structures experiencing large deformations or significant rotations.

**Stiffness Matrix Updating:** Iteratively updating the stiffness matrix based on the deformed geometry to capture changes in member stiffness.

**Load Redistribution:** Accounting for the redistribution of internal forces and moments due to second-order effects, which may affect the overall structural response and stability.

Buckling Considerations: Assessing the potential for structural instability or buckling under combined axial loads and lateral displacements.

## 1.3 Importance of P-delta Analysis:

P-delta analysis is important for several reasons:

Accuracy: Traditional linear analysis methods often neglect the effects of second-order deformations, leading to inaccuracies in predicting the behaviour of structures, especially in tall or slender structures subjected to significant loads. P-delta analysis provides a more accurate representation of structural response by considering these effects.

**Stability Assessment:** Second-order effects can significantly influence the stability of structures, especially those with high slenderness ratios or non-uniform load distributions. P-delta analysis helps engineers assess the stability of structures under various loading conditions and prevent potential buckling or instability issues.

**Code Compliance:** Many building codes and standards require engineers to consider secondorder effects in the analysis and design of structures, particularly for high-rise buildings, longspan bridges, and other complex structures. P-delta analysis ensures compliance with these regulations and helps engineers design safe and resilient structures.

**Redundancy Effects:** In statically indeterminate structures, second-order effects can lead to redistribution of internal forces and moments, affecting the load paths and overall structural behaviour. P-delta analysis accounts for these effects, enabling engineers to accurately predict the load distribution and assess the structural response under different loading scenarios.

**Dynamic Analysis:** P-delta effects become more significant in dynamic analysis, where the inertial forces interact with the deformed shape of the structure. Dynamic loads, such as wind or seismic loads, can amplify these effects, making it essential to include P-delta analysis in dynamic simulations to obtain realistic results.

**Performance-Based Design:** In performance-based design approaches, such as performance-based earthquake engineering (PBEE), accurately capturing second-order effects is crucial for assessing the performance of structures under extreme events and ensuring resilience against seismic hazards. P-delta analysis plays a key role in these advanced design methodologies.

# 1.4 Different Types of Analysis in Structural Engineering:

In structural engineering, various types of analysis are conducted to ensure that structures are safe, stable, and perform as intended under different load conditions. Here are the main types of structural analysis

## 1. Static Analysis

Linear Static Analysis: Assumes linear behaviour of materials and small displacements. Used for structures where loads are applied gradually and remain constant over time. It's the simplest form of analysis.

Nonlinear Static Analysis: Accounts for material nonlinearity (plasticity, cracking) and/or geometric nonlinearity (large displacements and deformations). Useful for assessing structures that undergo significant deformations.

## 2. Dynamic Analysis

Linear Dynamic Analysis: Used to study the behaviour of structures under dynamic loads (e.g., earthquakes, wind loads). Assumes linear material properties. Methods include modal analysis, response spectrum analysis, and time history analysis.

Nonlinear Dynamic Analysis: Considers nonlinear material properties and large deformations. It's more complex and computationally intensive, often used for accurate seismic performance evaluation.

## 3. P-Delta Analysis

P-Delta (P- $\Delta$ ) Analysis: A type of nonlinear static analysis that accounts for the additional moments induced by the vertical loads acting through the displaced position of the structure. Essential for tall buildings and structures susceptible to lateral displacements.

## 4. Buckling Analysis

Linear Buckling Analysis: Determines the critical load at which a structure becomes unstable. Assumes linear elastic behaviour up to the point of buckling.

Nonlinear Buckling Analysis: Considers both material and geometric nonlinearities. Provides a more accurate prediction of the buckling load and post-buckling behaviour.

# 5. Seismic Analysis

Equivalent Static Analysis: Simplified method for estimating seismic forces on a structure based on a static load equivalent to dynamic earthquake forces.

Dynamic Seismic Analysis: Includes response spectrum and time history analysis to account for the dynamic nature of seismic loads.

## 6. Frequency Analysis

Determines the natural frequencies and mode shapes of a structure, similar to modal analysis, but specifically focused on the response to cyclic or periodic loads.

## 7. Thermal Analysis

Assesses the effects of temperature changes on a structure. Includes thermal expansion/contraction, temperature gradients, and the resulting stresses and deformations.

## 8. Fire Analysis

Evaluates the structural response to high temperatures from fire. Considers material degradation and the effects of thermal expansion on structural stability.

## 9. Fluid-Structure Interaction (FSI) Analysis

Studies the interaction between a fluid (air, water) and a structure. Essential for designing structures subjected to fluid forces, such as bridges, offshore platforms, and tall buildings in high-wind areas.

Each type of analysis serves a specific purpose and provides critical insights into different aspects of structural behaviour. Engineers often use a combination of these analyses to ensure comprehensive assessment and robust design of structures. Understanding the appropriate type of analysis to apply in a given situation is crucial for ensuring the safety, stability, and performance of engineering projects.

## **OBJECTIVES**

## 2.1 General:

The P-delta analysis is a structural analysis technique used in the design of building structures, particularly tall or slender structures, to account for the effects of second-order (P-delta) effects. The primary objective of P-delta analysis is to consider the geometric nonlinearity in the structure's response to loads, especially vertical loads. The term "P-delta" refers to the combined effects of axial loads (P) and lateral loads (delta), where delta represents lateral displacements.

Here are the main objectives of P-delta analysis in building structures:

- Geometric Nonlinearity: P-delta analysis addresses the geometric nonlinearity of structures under lateral loads. In the analysis, the deformed shape of the structure is considered, leading to an iterative process to find the equilibrium configuration.
- **Stability and Equilibrium:** P-delta effects can lead to stability and equilibrium issues in tall or slender structures. By considering the P-delta effects, the analysis aims to ensure that the structure remains stable and in equilibrium under the applied loads.
- **Increased Accuracy:** The inclusion of P-delta effects provides a more accurate representation of the actual behaviour of the structure, especially in the presence of significant lateral loads. Ignoring these effects may lead to conservative or unrealistic results.
- **Member Stiffness Modification:** P-delta analysis involves modifying the stiffness of structural members based on the deformed shape of the structure. This modification accounts for the change in axial forces due to lateral displacements, providing a more accurate representation of member behaviour.
- Load Redistribution: P-delta effects can lead to the redistribution of loads within the structure. The analysis helps in understanding how the lateral displacements influence the distribution of forces and moments in different parts of the structure.
- Code Compliance: Many design codes and standards require the consideration of P-delta effects in the analysis of tall or flexible structures. Performing P-delta analysis ensures compliance with these codes and helps in designing structures that meet safety and performance criteria.

## 2.3 Benefits of P-delta Analysis:

P-Delta analysis provides several benefits in the field of structural engineering, particularly in the design and assessment of structures subjected to lateral loads. Here are the key benefits:

- Accurate Stability Evaluation: P-Delta analysis accounts for second-order effects due to lateral displacements, providing a more accurate assessment of structural stability compared to first-order analysis.
- Critical Load Determination: Helps in identifying critical loads that may lead to instability or failure, ensuring the structure can withstand anticipated loads without buckling.
- Nonlinear Effects: Incorporates geometric nonlinearity, which is essential for understanding the real behaviour of tall and slender structures under significant lateral loads.
- Load-Displacement Relationship: Provides a more accurate load-displacement relationship, capturing the effects of axial loads on the stiffness and stability of the structure.
- Regulatory Requirements: Meets the requirements of modern building codes and standards that mandate second-order analysis for certain types of structures, ensuring compliance and approval.
- Design Validation: Validates design assumptions and ensures that the structure adheres to the latest engineering practices and safety regulations.
- Failure Prevention: Helps in identifying potential failure modes related to lateral displacements and P-Delta effects, enabling proactive design modifications to mitigate risks.
- Performance-Based Design: Supports performance-based design approaches where structural performance under various load scenarios is critically assessed and optimized.
- Optimized Member Sizes: Allows for the optimization of member sizes by understanding the true demands on the structure, potentially leading to material and cost savings.
- Safety and Reliability: Enhances the safety and reliability of the structure by ensuring that it can resist both primary and secondary effects of loads.

## **LITERATURE REVIEW**

#### 3.1 General:

A literature review is an overview of the previously published works on a topic. The term can refer to a full scholarly paper or a section of a scholarly work such as a book, or an article. Either way, a literature review is supposed to provide the researcher/author and the audiences with a general image of the existing knowledge on the topic under question. A good literature review can ensure that a proper research question has been asked and a proper theoretical framework and/or research methodology have been chosen. To be precise, a literature review serves to situate the current study within the body of the relevant literature and to provide context for the reader. In such case, the review usually precedes the methodology and results sections of the work.

#### • Regina Gaiotti and Bryan Stafford Smith, (1989)

The trend towards more slender and lighter building structures has resulted in potentially more significant *P*-delta effects; this has led to the demand for simple and accurate methods of *P*-delta analysis. Methods are reviewed and compared in terms of their efficiency and accuracy. Considered roughly in their order of sophistication, the methods reviewed include the amplification factor method, the direct method, the iterative method, the negative property member methods, and the second-order computer program method. In addition to these, a new method similar to the iterative method, but based on analyses using the actual gravity loading applied to successive deflected shapes, is presented. The results are identical to those given by the iterative method, while the analysis takes less than one-third of the time. Factors that differentiate the methods include their accuracy, ease of use, whether they are for hand or computer use, and whether they are applicable to all types of structures or only to certain types.

1. The negative property column method is the best method for accessing P-Delta Analysis.

2. Second-order effects due to column bending are rarely significant in practical structures.

#### • E. L. Wilson, and A. Habibullah, (1987)

The P-Delta phenomenon is an area of concern to structural engineers. Traditional methods for incorporating P-Delta effects in analysis are based on iterative techniques. These techniques are time-consuming and are in general used for static analysis only. For building structures, the mass, which causes the P-Delta effect, is constant irrespective of the lateral loads and displacements. This information is used to linearize the P-Delta effect for buildings and solve the problem "exactly", satisfying equilibrium in the deformed position, without iterations. An

algorithm is developed that incorporates the P-Delta effects into the basic formulation of the structural stiffness matrix as a geometric stiffness correction. This procedure can be used for both static and dynamic analysis and will account for the lengthening of the structural time periods and changes in mode shapes due to P-Delta effects. The algorithm can be directly incorporated into building analysis programs.

- 1. The changes in the displacements and member forces are less than 10%.
- 2. P-Delta effects can equally affect both translation and torsion.

## • Avigdor Rutenberg, (1981)

A simple technique is proposed that enables a direct second order analysis to be performed by means of first order plane frame computer programs. The geometric-stiffness matrix is modelled as a fictitious column with negative stiffness. The effect of additional moments due to eccentricity of axial force about the deflected shape is considered. The approach is also applicable to three dimensional problems and can also be used with nonlinear computer programs to evaluate the effect of sway on elastic-plastic frames.

1. The second order effects are either assumed proportional to the first order ones, or are evaluated on the basis of some approximation to the stiffness of the storey.

#### • Mallikarjuna B.N, Ranjith A, (2014)

The high rise buildings require high frame structure stability for safety and design purposes. This research focused on P -delta analysis to be compared with linear static analysis. In this study, a 18 storey steel frame structure with 68.9 m has been selected to be idealized as multi storey steel building model. The model is analysed by using STAAD.Pro 2007 structural analysis software with the consideration of P-delta effect. At the same time the influence of different bracing patterns has been investigated. For this reason five types of bracing systems including X, V, Single Diagonal, Double X, K bracing with unbraced model of same configuration are modelled and analysed. The framed structure is analysed for Wind load as per IS 875 (part 3)-1987. After analysis, the comparative study is presented with respective to Maximum storey displacement and Axial Force. The present work showed that the 'X' bracing in continuous bracing pattern is proved to be more effective with respect to both Static and P-delta analysis.

- 1. The second order effects found to increase the storey displacements at all level of the structure. Compare to the structure subjected to other than second order effects.
- 2. The value of Axial Force in P-delta analysis is twice more than compared to static analysis.

# **METHODOLOGY**

## 4.1 General:

In its most common sense, methodology is the study of research methods. However, the term can also refer to the methods themselves or to the philosophical discussion of associated background assumptions. A method is a structured procedure for bringing about a certain goal, like acquiring knowledge or verifying knowledge claims. This normally involves various steps, like choosing a sample, collecting data from this sample, and interpreting the data. The study of methods concerns a detailed description and analysis of these processes. It includes evaluative aspects by comparing different methods. This way, it is assessed what advantages and disadvantages they have and for what research goals they may be used. These descriptions and evaluations depend on philosophical background assumptions.

## 4.2 Process of Project:

#### • Define the Structure:

Start by defining the geometry and properties of the structure in STAAD.Pro. Input information such as nodes, elements, supports, materials, and member properties.

#### • Specify Loads:

Specify the applied loads on the structure. Include gravity loads, lateral loads, and any other relevant loads.

#### • Specify Analysis Parameters:

Set up the analysis parameters in STAAD.Pro. This includes specifying the type of analysis (e.g., linear or nonlinear), load factors, and convergence criteria.

#### • Perform Linear Analysis:

Before conducting the P-delta analysis, perform a linear analysis to determine the initial structure's response to applied loads.

#### • Enable P-Delta Analysis:

To include P-delta effects, enable the P-delta analysis option in STAAD.Pro. This is typically found in the analysis settings or options.

#### • Specify P-Delta Parameters:

Define P-delta parameters such as convergence criteria, iteration limits, and other settings. These parameters control the accuracy and convergence of the P-delta analysis

#### • Run P-Delta Analysis:

Run the P-delta analysis in STAAD.Pro. This analysis will consider the interaction between axial loads and lateral displacements, providing a more accurate representation of the structure's behaviour.

## • Review Results:

Examine the analysis results, including member forces, deformations, and reactions. Pay attention to how P-delta effects influence the overall structural response.

## • Iterate if Necessary:

Depending on the analysis results, you may need to iterate and refine the model. Adjust parameters as needed to achieve convergence and accurate results.

## • Check Code Compliance:

Ensure that the structure satisfies the relevant design codes and standards, taking P-delta effects into account.

# 4.3 Challenges:

## 1. Convergence Issues:

P-delta analysis involves an iterative process, and achieving convergence can be challenging, especially for highly nonlinear systems. Convergence issues may require adjusting analysis settings, such as convergence tolerances and iteration limits.

## 2. Modelling Complexity:

Complex building structures with irregular geometries, varying member properties, and multiple load conditions can make it challenging to create an accurate model for P-delta analysis. Properly representing the structure's geometry and material properties is crucial for meaningful results.

## 3. Dynamic Effects:

P-delta analysis is typically performed under static loading conditions. However, for dynamic or seismic loads, the dynamic effects need to be considered, adding complexity to the analysis. This may involve coupling with dynamic analysis methods.

## 4. Software Limitations:

The accuracy of P-delta analysis is also dependent on the capabilities of the structural analysis software being used. Some software may have limitations in handling certain types of structures or may not provide advanced features for addressing specific P-delta effects.

#### 5. Member Releases and Supports:

Introducing member releases or supports in the structure, which is common in real-world structures, can complicate P-delta analysis. The correct implementation of releases and supports is crucial for accurate results.

## 6. Material and Geometric Nonlinearity:

P-delta effects arise from the interaction of axial loads with lateral displacements, introducing material and geometric nonlinearity. Modelling these nonlinearities accurately is essential, and neglecting them can lead to inaccurate results.

## 7. User Understanding and Expertise:

P-delta analysis requires a good understanding of structural behaviour, numerical methods, and the specific features and settings within the analysis software. Inadequate user expertise may result in misinterpretation of results or inappropriate model adjustments.

#### 8. Computational Intensity:

P-delta analysis is computationally more intensive than linear analysis, and it may require additional computational resources. Large models or structures with a high degree of complexity may demand substantial computational time and power.

#### 9. Sensitivity to Initial Conditions:

P-delta analysis can be sensitive to initial conditions and assumptions made during the analysis setup. Small changes in these conditions may lead to significant variations in results.

#### **10. Code Compatibility:**

Ensuring that P-delta analysis complies with relevant design codes and standards adds an additional layer of complexity. Different codes may have varying requirements for considering P-delta effects.

# 4.4 Software Used:

**STAAD.Pro CONNECT Edition V22:** STAAD.Pro stands as a premier software solution for structural analysis and design, renowned for its comprehensive suite of tools tailored to meet the demands of modern engineering projects. Developed by Bentley Systems, this robust platform offers engineers unparalleled versatility in modelling, analyzing, and visualizing various types of structures. With intuitive modelling capabilities, STAAD.Pro enables users to effortlessly generate detailed 3D models of buildings, bridges, towers, and other structural systems, empowering them to accurately represent real-world scenarios. Its advanced analysis features encompass linear and nonlinear static analysis, dynamic analysis, finite element analysis (FEA), P-delta analysis, and seismic analysis, ensuring engineers have the tools necessary to evaluate structural performance under diverse loading conditions.

Moreover, STAAD.Pro seamlessly integrates design modules for concrete, steel, timber, aluminium, and cold-formed steel structures, facilitating code-based design checks and optimization of structural members. This interoperable software platform fosters collaboration among multidisciplinary project teams by supporting integration with CAD software, BIM platforms, and third-party analysis tools. With automation capabilities and scripting tools, engineers can streamline workflows, customize tasks, and enhance productivity, making STAAD.Pro an indispensable asset in the arsenal of modern engineering professionals.

# **OBSERVATION AND CALCULATION**

# 5.1 General:

This chapter deals with the studies and analysis carried out on the structure using a series of load combinations consisting of dead load, live load, wind load and seismic load. The results are obtained after considering the geometric non-linearity caused due to the horizontal displacement caused due to the prevailing wind loads and seismic loads.

# **5.2 Specifications:**

A typical frame structure has been used for this project including a set of beams and columns to make a frame, wherein 9 columns and 6 beams have been used with the following specifications:

Description	Horizontal Beam	Vertical Column	
Length	5m	3m	
Properties	W10X60	W8X10	
Materials	STEEL_344737.86_kN/m <sup>2</sup>	STEEL_344737.86_kN/m <sup>2</sup>	

	Table	5.1	.1:	Sp	ecific	ations
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(Note: 3 Fixed supports used at the end of vertical columns.)



# 5.3 Loads:

The following load cases were considered to be acted upon the structure for the preferred results of the project

**Dead Load** = 1KN/m

Live Load = 10kN/m

**Self Weight** = 1KN/m

#### Seismic Load

- Topmost three nodes = 150 kN-m acting rightward
- Middle three nodes = 150 kN-m acting rightward
- Bottom three nodes = 150 kN-m acting rightward

#### Wind Load

• In X Winward Force

Top left Vertical Column = force acting on Y axis with a range of (6m min to 9m max).

• In -X Leeward Force

Top right Vertical Column = force acting on Y axis with a range of (6m min to 9m max).

= force acting on X axis with a range of (10m min to 10m max).

(Note: Wind Load is calculated as per ASCI 7-Part 16 with the building category taken as I and basic wind speed to be at 33 m/sec as per IS 875-Part 3 as the wind zone is taken as I and the exposure for the structure is taken as category B indicating Urban and Sub Urban areas).

(Note: Seismic Load is distributed equally among all the floors as per stated by ASCE 7-Part 16).

## **RESULTS**

## 6.1 General:

The presentation of results obtained after the analysis of the structure under different load combinations. In this analysis only a framed structure was considered as the whole modern building structure is based on framed structure consisting of beams and columns. Hence the motive of this project was to imply elementary p-delta analysis and get the results of the framed structure.

The following graphs were plotted using the values obtained after the completion of P-delta analysis of the structure:

#### **6.2 DEFLECTION:**

Deflection, in structural engineering and physics, refers to the degree to which a structural element is displaced under a load. It is a critical factor in the design and analysis of structures, ensuring that buildings, bridges, and other constructions can withstand various forces without excessive bending or deformation. The amount of deflection is influenced by the material properties, the geometry of the element, and the type of load applied. Accurate calculation and control of deflection are essential to maintain the integrity and safety of structures, preventing failures and extending their lifespan. Understanding deflection helps engineers design more resilient structures that can endure environmental stresses and daily usage.



#### • Deflection Graph for Y-max Direction

Graph 6.2.1: Deflection graph for Y-max direction

**Description of the Graph:** This graph is the representation of each node's respective maximum deflection (in the direction of Y-axis), under the applied loads. As the nodes numbered 1, 2, 3; are supports and hence, there are no specific deflection in these nodes therefore no values are provided for the mentioned three nodes.



#### • Deflection Graph for Y-min Direction

Graph 6.2.2: Deflection graph for Y-min direction

**Description of the Graph:** This graph is the representation of each node's respective Minimum deflection (in the direction of Y-axis), under the applied loads. As the nodes numbered 1, 2, 3, are supports hence there are no specific deflection in these nodes therefore no values are provided for the mentioned three nodes.

#### • Deflection Graph for X-Direction



Graph 6.2.3: Deflection graph for X-direction

**Description of the Graph:** This graph is the representation of each node's respective Maximum deflection (in the direction of X-axis), under the applied loads. As the nodes numbered 1, 2, 3, are supports hence there are no specific deflection in these nodes therefore no values are provided for the mentioned three nodes.

## **6.3 AXIAL FORCE:**

Axial force is a fundamental concept in structural engineering and mechanics, referring to the force applied along the longitudinal axis of a structural member, such as a column, beam, or rod. This type of force can either be tensile, stretching the member, or compressive, shortening it. Understanding axial force is crucial for ensuring that structures can support loads without undergoing structural failure, such as buckling or fracturing. Accurate assessment of axial forces allows engineers to design components that can efficiently bear loads, distribute stresses appropriately, and maintain overall stability and safety of constructions ranging from buildings and bridges to mechanical systems and vehicles.



#### • Graph for Maximum Axial Forces for Dead Load (Fx)

Graph 6.3.1: Graph for maximum axial forces for dead load (Fx)

**Description of the Graph:** This graph is the representation of each beam's respective Maximum axial force under the applied loads (i.e. dead load only in this case). (In this graph there is minimum values in beam 1 following till 7 and a hike in values from beam 8 following till 15 this is because the first seven are beams and the latter are column due to which there is a variation in the values of axial force).



• Deflection for Maximum Axial Forces for Combination of Loads (Fx)

Graph 6.3.2: Graph for maximum axial forces for combination of loads (Fx)

**Description of the Graph:** This graph is the representation of each beam's respective Maximum axial force under the combination of loads.

#### **6.4 BENDING MOMENT:**

A bending moment is a critical concept in structural engineering, representing the internal moment that induces bending within a structural element when subjected to external forces or loads. This moment is a measure of the tendency of a force to cause rotation about a point or axis and is crucial in the design and analysis of beams, girders, and other structural members. Understanding bending moments helps engineers determine how loads will affect the shape and stability of a structure, ensuring that it can withstand applied stresses without excessive deformation or failure. Accurate calculation of bending moments allows for the design of safe, efficient, and durable structures that can support various loads over their intended lifespan.



#### • Graph for Maximum Bending Moments for Dead Load (Mz)

Graph 6.4.1: Graph for maximum bending moment for dead load (Mz)

**Description of the Graph:** This is a graph showing the max bending moment occurring in the structure due to dead load only, where we can see that the first 6 beams are horizontal beams in the structure hence the greater values of bending moment can be seen whereas the latter 9 beams are vertical column hence less value of bending moment within, which beams numbered 8, 11, 14 fall on the centre of gravity of the structure due to which the values on these are zero.

• Graph for Maximum Bending Moments for Combination Load (Mz)



Graph 6.4.2: Graph for maximum bending moment for combination load (Mz)

**Description of the Graph:** This is a graph showing the max bending moment occurring in the structure due to combination load due to which we can see values even in columns as there are horizontal wind and seismic loads acting on them.

# **FUTURE SCOPE**

#### 1. Advanced Numerical Techniques:

Continued advancements in numerical methods and algorithms may lead to more efficient and robust P-delta analysis techniques. Researchers may explore novel approaches to address convergence issues and enhance the accuracy of the analysis.

#### 2. Machine Learning and Artificial Intelligence:

The application of machine learning and artificial intelligence in structural analysis could potentially aid in automating certain aspects of P-delta analysis. Smart algorithms may help optimize model parameters, identify critical areas for refinement, and assist in achieving convergence more efficiently.

#### 3. Cloud-Based Computing:

Utilizing cloud-based computing resources can offer substantial computational power for complex P-delta analyses. This approach may enable engineers to analyse larger and more intricate structures without being constrained by local computational resources.

#### 4. User-Friendly Interfaces:

Future developments may focus on creating more user-friendly interfaces for P-delta analysis software. Intuitive interfaces with guided workflows and built-in assistance could make it easier for engineers to set up and interpret P-delta analyses.

#### 5. Improved Visualization Tools:

Enhancements in visualization tools may help engineers better understand the results of P-delta analyses. 3D visualizations, animations, and interactive displays could provide clearer insights into the structural behaviour under lateral loads.

#### 6. Dynamic P-Delta Analysis:

Future developments may explore dynamic P-delta analysis methods, particularly for structures subjected to dynamic loads such as earthquakes or wind. This could involve incorporating time-dependent effects and considering the interaction between dynamic responses and P-delta effects.

## **CONCLUSION**

In conclusion, P-delta analysis plays a crucial role in the accurate assessment of building structures, particularly when subjected to lateral loads. The consideration of P-delta effects addresses the geometric nonlinearity that arises from the interaction between axial loads and lateral displacements. This analysis is essential for tall or slender structures where the influence of second-order effects becomes significant.

The challenges associated with P-delta analysis, such as convergence issues, modelling complexity, and computational intensity, highlight the need for careful consideration and expertise in the analysis process. Despite these challenges, P-delta analysis remains a fundamental step in ensuring the structural integrity, stability, and safety of buildings.

Looking towards the future, advancements in numerical techniques, the application of machine learning, and improved user interfaces are expected to enhance the efficiency and accessibility of P-delta analysis. Additionally, the potential for dynamic P-delta analysis and increased automation in model setup could further refine the accuracy of predictions, allowing for a more comprehensive understanding of structural behaviour under various loading conditions.

Ultimately, the continued development and refinement of P-delta analysis methodologies contribute to the ongoing evolution of structural engineering practices. Engineers must stay abreast of advancements in analysis techniques, leverage emerging technologies, and collaborate with software developers to ensure that P-delta analysis remains a reliable and effective tool for designing safe and resilient building structures.

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